



- Find the transfer function $C(s)/R(s)$ for the following control system shown in Fig. (1):
 - Using block reduction method.
 - Using signal flow graph.
- Determine the transfer function $E_o(s)/E_i(s)$ of the circuit shown in Fig. (2) and then draw the block diagram.

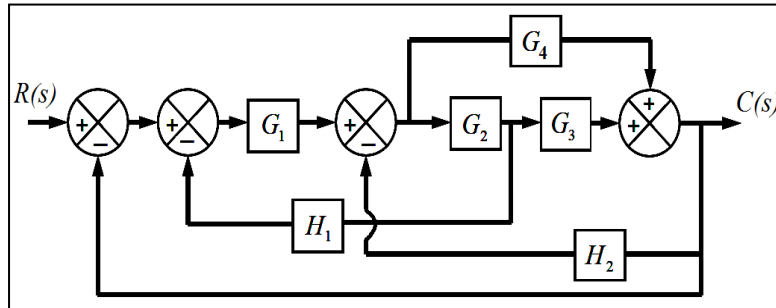


Fig. (1)

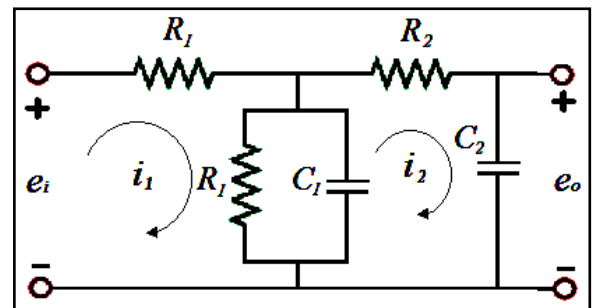


Fig. (2)



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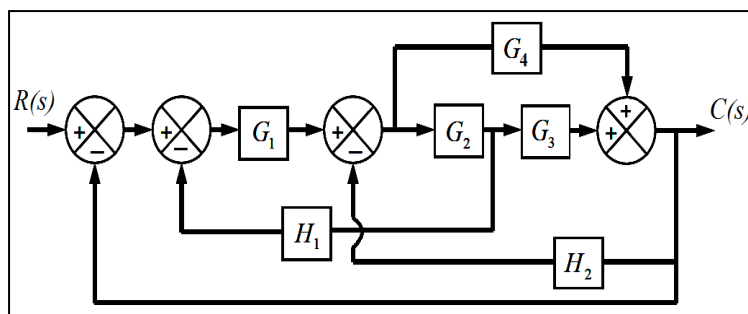


Fig. (1)

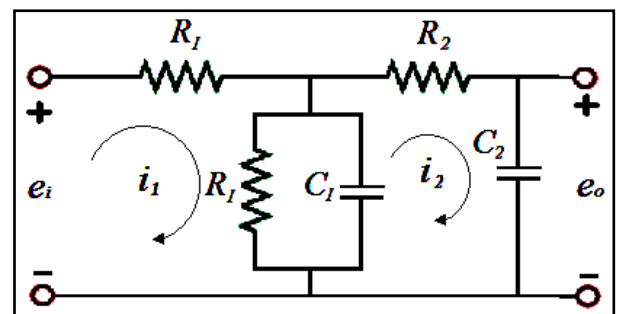


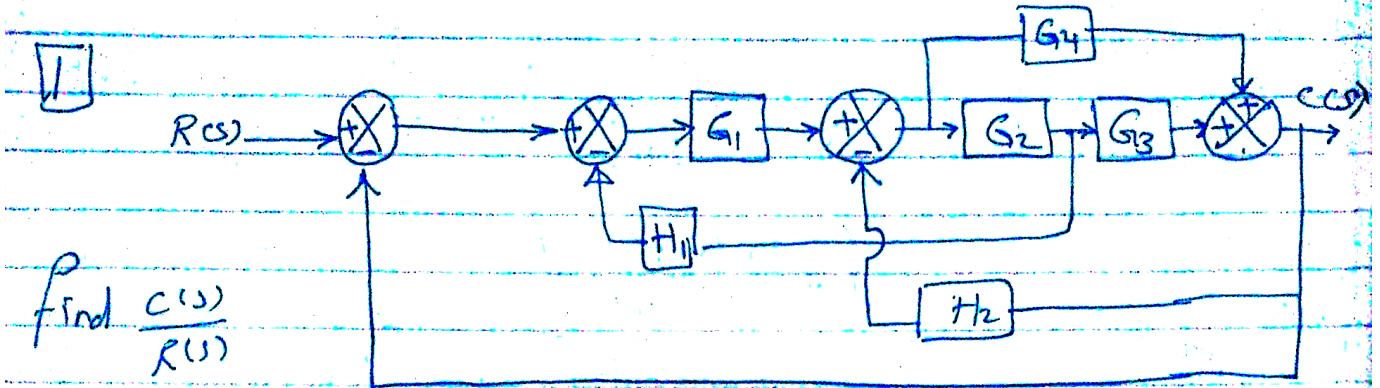
Fig. (2)



Automatic Control 3rd Comp 2016-2017
 1st Term

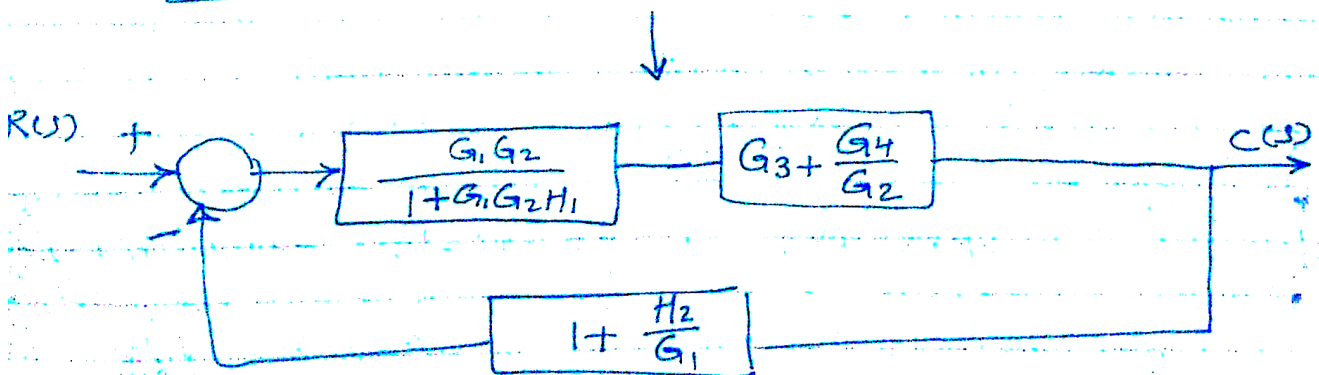
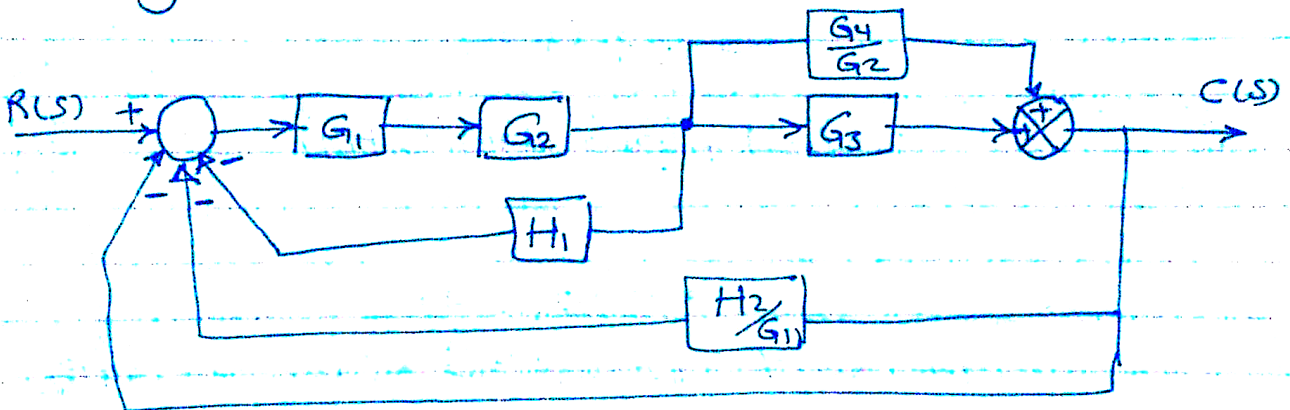
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" Model Answer "



find $\frac{C(s)}{R(s)}$

(i) using block reduction Method:

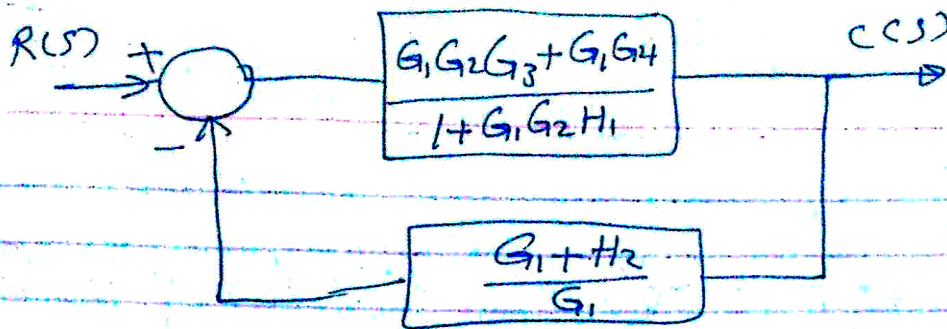


$$\therefore \frac{G_1 G_2}{1 + G_1 G_2 H_1} * \frac{G_2 G_3 + G_4}{G_2} = \frac{G_1 G_2 G_3 + G_1 G_4}{1 + G_1 G_2 H_1}$$

$$\therefore 1 + \frac{H_2}{G_1} = \frac{G_1 + H_2}{G_1}$$



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$$\begin{aligned} \text{So } \frac{C(s)}{R(s)} &= \frac{\left(\frac{G_1 G_2 G_3 + G_1 G_4}{1 + G_1 G_2 H_1} \right)}{1 + \left(\frac{G_1 G_2 G_3 + G_1 G_4}{1 + G_1 G_2 H_1} \right) * \left(\frac{G_1 + H_2}{G_1} \right)} \\ &= \frac{G_1 G_2 G_3 + G_1 G_4}{1 + G_1 G_2 H_1 + (G_2 G_3 + G_4)(G_1 + H_2)} \\ &= \frac{G_1 G_2 G_3 + G_1 G_4}{1 + G_1 G_2 H_1 + G_1 G_2 G_3 + G_1 G_4 + G_2 G_3 H_2 + G_4 H_2} \end{aligned}$$

$$\text{So } \frac{C(s)}{R(s)} = \frac{(G_1 G_2 G_3 + G_1 G_4)}{1 + (G_1 G_2 G_3 + G_1 G_4) + G_1 G_2 H_1 + (G_2 G_3 + G_4) H_2}$$

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(ii) Using signal flow Graph.

$$L_1 = -G_1 G_2 H_1$$

$$L_2 = -G_1 G_4$$

$$L_3 = -G_1 G_2 G_3$$

$$L_4 = -G_4 H_2$$

$$L_5 = -G_2 G_3 H_2$$

$$\begin{aligned}\Delta &= 1 + G_1 G_2 H_1 + G_1 G_4 + G_1 G_2 G_3 + G_4 H_2 + G_2 G_3 H_2 \\ &= 1 + G_1 G_2 G_3 + G_1 G_4 + G_1 G_2 H_1 + (G_2 G_3 + G_4) H_2\end{aligned}$$

$$P_1 = G_1 G_2 G_3 \quad (\Delta_1 = 1)$$

$$P_2 = G_1 G_4 \quad (\Delta_2 = 1)$$

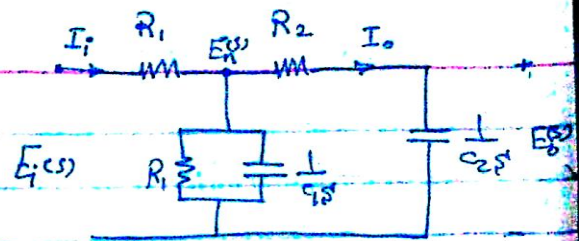
$$\therefore \frac{C(s)}{R(s)} = \frac{G_1 G_2 G_3 + G_1 G_4}{1 + G_1 G_2 G_3 + G_1 G_4 + G_1 G_2 H_1 + (G_2 G_3 + G_4) H_2}$$

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(4)

find $\frac{E_o(s)}{E_i(s)} = ?$



$$Z_1 = \frac{R_1 \cdot \frac{1}{C_1 s}}{R_1 + \frac{1}{C_1 s}} = \frac{R_1}{1 + R_1 C_1 s}$$

$$Z_2 = \frac{Z_1 (R_2 + \frac{1}{C_2 s})}{Z_1 + (R_2 + \frac{1}{C_2 s})} = \frac{R_1 + R_1 R_2 C_2 s}{1 + R_1 C_1 s + R_2 C_2 s + R_1 R_2 s^2 + R_1 R_2 C_2 s^2}$$

Voltage divider Rule:

$$* \frac{E_n(s)}{E_i(s)} = \frac{Z_2}{R_1 + Z_2} \quad \text{--- (1)}$$

$$* \frac{E_o(s)}{E_n(s)} = \frac{(\frac{1}{C_2 s})}{R_2 + \frac{1}{C_2 s}} = \frac{1}{1 + R_2 C_2 s} \quad \text{--- (2)}$$

Multiply (1) by (2) To get $\frac{E_o(s)}{E_i(s)}$

$$\frac{E_o(s)}{E_i(s)} =$$

Not that $E_i(s) = I_i(s) * (R_1 + Z_2)$
 $E_n(s) = I_i(s) * Z_2$
 $E_o(s) = I_o(s) * (\frac{1}{C_2 s})$
 $E_i(s) = I_o(s) * (R_2 + \frac{1}{C_2 s})$

$$= \frac{R_1 + R_1 R_2 C_2 s}{2 R_1^2 + R_1^2 C_1^2 s^2 + R_1^2 R_2^2 C_1 C_2^2 s^3 + R_1^2 R_2 C_2^2 s^2 + 2 R_1 R_2^2 C_2^2 s^2 + 2 R_1^2 R_2 C_1 C_2 s^2 + 4 R_1 R_2 C_2 s}$$

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